

Assignment # 02:-

**NUMERICALS:-**

① One gram of a certain polar substance is dissolved into  $1000\text{cm}^3$  of nonpolar liquid. The liquid itself has dielectric constant of 3 at  $27^\circ\text{C}$ . whereas solution has dielectric constant of 3.2 at the same temperature. Calculate dipole moment?

**Sol:-**

Volume is assumed to be constant after dissolving polar substance in liquid.

$$N\alpha_e = 3\epsilon_0 \left[ \frac{\epsilon_r - 1}{\epsilon_r + 2} \right]$$

$$'' = 3\epsilon_0 \left[ \frac{3 - 1}{3 + 2} \right] \text{ for liquid.}$$

$$N\alpha_e + N_2\alpha_0 = 3\epsilon_0 \left[ \frac{\epsilon_r - 1}{\epsilon_r + 2} \right]$$

$$'' = 3\epsilon_0 \left[ \frac{3.2 - 1}{3.2 + 2} \right] \text{ for solution.}$$

$$N_2\alpha_0 = 3\epsilon_0 \left[ \frac{2.2}{5.2} \right] - 3\epsilon_0 \left[ \frac{2}{5} \right]$$

$$'' = 3\epsilon_0 \left[ \frac{2.2}{5.2} - \frac{2}{5} \right]$$

$$\alpha_0 = \frac{3\epsilon_0}{N} [0.423 - 0.4]$$

$$\alpha_0 = \frac{N_0^2}{3k_B T} = \frac{3\epsilon_0}{N_2} [0.43 - 0.4]$$

$$N_0^2 = \frac{9k_B T \epsilon_0}{N_2} \cdot 0.023$$

$$M = \mu$$

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$$H_0 = \frac{9 \times 1.38 \times 10^{-23} \times 300 \times 8.85 \times 10^{-12} \times 0.023}{6.02 \times 10^{26}}$$

$$H_0 = 0.355 \times 10^{-29} \text{ C.m.}$$

② A parallel plate capacitor has area of  $8 \text{ cm}^2$  with separation of  $0.08 \text{ mm}$ , the space is filled with polystyrene. The real part of relative dielectric constant is  $2.56$  and loss tangent is  $0.7 \times 10^{-4}$  at frequency of  $1 \text{ MHz}$ . Calculate capacitance & equivalent loss resistance.

Sol:- Area of parallel plate capacitor is

$$8 \text{ cm}^2 = 8 \times 10^{-4} \text{ m}^2$$

$$\cdot \text{separation} = d = 0.08 \text{ mm.}$$

$$\cdot \text{dielectric constant} = k = 2.56.$$

$$\cdot \text{loss tangent} = \tan \delta = 0.7 \times 10^{-4}$$

$$\cdot \text{Frequency} = 1 \text{ MHz} = 1 \times 10^6 \text{ Hz}$$

Capacitance of parallel plate is:

$$C = \frac{k \epsilon_0 A}{d} = \frac{2.56 \times 8.85 \times 10^{-12} \times 8 \times 10^{-4}}{0.08 \times 10^{-3}}$$

$$C = 2.26 \times 10^{-10} \text{ F}$$

The capacitive reactance of circuit =  $X_c = \frac{1}{2\pi f C}$

$$\tan \delta = R / X_c$$

$$R = X_c \tan \delta$$

$$R = \frac{\tan \delta}{2\pi f C}$$

$$R = \frac{0.7 \times 10^{-4}}{2 \times 3.14 \times 1 \times 10^6 \times 2.26 \times 10^{-10}}$$

$$R = 0.49 \Omega$$

$$R = 49 \times 10^{-3} \Omega$$

$$R = 49 \times 10^{-3} \Omega$$

equivalent to parallel loss resistance

Exclusive  
Falcon

3) The bakelite is found to have real part of its complex relative dielectric constant as 4.36 with loss tangent  $2.8 \times 10^{-2}$  at frequency 1 MHz. Calculate complex polarizability of material assuming Lorentz field given  $N = 4 \times 10^{29}$

Sol:-

The relation b/w  $\epsilon_r^*$  and  $\alpha^*$  is similar to Clausius-Mosotti expression and given as

$$\frac{\epsilon_r^* - 1}{\epsilon_r^* + 2} = \frac{N \alpha^*}{3 \epsilon_0}$$

where  $\epsilon_r^* = \epsilon_r' - i \epsilon_r''$

$$\tan \delta = \frac{\epsilon_r''}{\epsilon_r'}$$

$$\epsilon_r'' = \epsilon_r' \tan \delta$$

$$\begin{aligned} \text{Hence } \epsilon_r^* &= \epsilon_r' - i \epsilon_r' \tan \delta \\ &= \epsilon_r' (1 - i \tan \delta) \end{aligned}$$

$$\epsilon_r' = 4.36$$

$$\tan \delta = 0.028$$

$$N = 4 \times 10^{29}$$

$$\epsilon_0 = 8.85 \times 10^{-12}$$

$$\frac{\epsilon_r^* - 1}{\epsilon_r^* + 2} = \frac{N \alpha^*}{3 \epsilon_0}$$

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$$\frac{3.36 - 0.12208i}{6.36 - 0.12208i} = \frac{4 \times 10^{29} \times \alpha^x}{3 \times 8.85 \times 10^{-12}}$$

~~21.3845~~

$$\frac{(3.36 - 0.12208i)(6.36 + 0.12208i)}{(6.36 + 0.12208i)(6.36 - 0.12208i)} = 156.8 \times 10^{37} \alpha^x$$

$$\frac{21.3845 + i[-0.36624]}{40.465} = 150.79 \times 10^{37} \alpha^x$$

$$\alpha^x = \frac{21.3845 - i0.36624}{6.1017 \times 10^{40}}$$

$$\alpha^x = (3.5 - i0.06) \times 10^{-40}$$

$$\alpha_1^x = 10^{-40} \times (3.5 - i0.06)$$

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Assignment II :- Problems.

6) Calculate the probability that a quantum state in conduction band at  $E = E_c + kT/2$  is occupied by an electron, Calculate Thermal equilibrium electron concentration is silicon at  $T = 300\text{K}$ ?

Sol:- The Probability that an quantum state at  $E = E_c + kT/2$  is occupied by electron is given by :-

$$f_f(F) = \frac{1}{1 + \exp\left(\frac{E - E_f}{kT}\right)} \approx \exp\left[-\frac{E - E_f}{kT}\right]$$

putting  $E = (E_c + kT/2)$

$$f_f(F) = \exp\left[-\frac{E_c + kT/2 - E_f}{kT}\right]$$

$$f_f(F) = \exp\left[\frac{-(0.25) + (0.0259)/2}{0.0259}\right]$$

$$E = 300\text{K}$$
$$N_c = 2.5 \times 10^{19} \text{cm}^{-3}$$

$$" = 3.90 \times 10^{-5}$$

The electron concentration is given by

$$n_0 = N_c \exp\left[-\frac{(E_c - E_f)}{kT}\right]$$

$$" = (2.8 \times 10^{19}) \exp\left[\frac{-0.25}{0.0259}\right]$$

$$" = 1.80 \times 10^{15} \text{cm}^{-3}$$

7) Calculate the thermal equilibrium hole concentration in silicon at  $T = 300\text{K}$ . Assume that fermi energy is  $0.277\text{eV}$  above valance band energy. The value of  $N_v$  for silicon at  $T = 300\text{K}$  is  $N_v = 1.04 \times 10^{19}$

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Sol:- we have formula:-

$$\frac{N_{v2}}{N_{v1}} = \left(\frac{T_2}{T_1}\right)^{3/2}$$

$$N_{v2} = N_{v1} \left(\frac{T_2}{T_1}\right)^{3/2}$$

$$" = 1.04 \times 10^{19} \text{ cm}^{-3} \left(\frac{400\text{K}}{300\text{K}}\right)^{3/2}$$

$$" = 1.60 \times 10^{19} \text{ cm}^{-3}$$

The hole concentration is

$$p_0 = N_v \exp\left[-\frac{E_f - E_v}{kT}\right]$$

$$E_f - E_v = 0.27 \text{ eV}$$

$$= 0.27 \times 1.6 \times 10^{-19}$$

$$p_0 = (1.60 \times 10^{19}) \exp\left[-\frac{0.27 \times 1.6 \times 10^{-19}}{1.38 \times 10^{-23} \times 400}\right]$$

$$1.38 \times 10^{-23} \times 400$$

$$p_0 = 6.43 \times 10^{15} \text{ cm}^{-3}$$

Q Calculate the intrinsic carrier concentration in silicon at  $T = 250\text{K}$  and  $T = 400\text{K}$ . The values of  $N_c$  and  $N_v$  for silicon at  $T = 300\text{K}$  are  $2.8 \times 10^{19} \text{ cm}^{-3}$  and  $1.04 \times 10^{19} \text{ cm}^{-3}$  respectively. Both  $N_c$  and  $N_v$  vary at  $T^{3/2}$ . Assume the bandgap energy of silicon is  $1.12 \text{ eV}$  and does not vary over temperature ranges.

Sol:- we have formula.

$$n_i^2 = N_c N_v \exp\left[-\frac{E_c - E_v}{kT}\right] = N_c N_v \left[\frac{E_g}{kT}\right]$$

$$" = (2.8 \times 10^{19})(1.04 \times 10^{19}) \left(\frac{250}{300}\right)^3 \exp\left[\frac{-1.12}{(0.0259) \left(\frac{250}{300}\right)}\right]$$

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$$n_i^2 = 4.90 \times 10^{15}$$

$$n_i = 7.0 \times 10^7 \text{ cm}^{-3}$$

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For an intrinsic semiconductor with gap  $E_g = 0.7 \text{ eV}$ , determine position of fermi level at  $T = 300 \text{ K}$  if  $m_p^* = 6m_e^*$ . Also calculate density of holes and electrons at  $300 \text{ K}$ . How do quantities alter if  $E_g = 7 \text{ eV}$ ?

Soln -  $E_g = 0.7 \text{ eV}$

$$n = N_c e^{-(E_c - E_f)/kT}$$

$$p = N_v e^{-(E_f - E_v)/kT}$$

$$p = n$$

$$N_c = e^{-(E_c - E_f)/kT} = N_v e^{-(E_f - E_v)/kT}$$

$$N_c = \frac{m_p}{kT} \quad N_v = \frac{m_p}{kT}$$

$$m/e e^{-(E_c - E_f)/kT} = \frac{m}{e} e^{-(E_c - E_v)/kT}$$

$$E_c - E_v = E_g$$

$$\frac{1}{6} = e^{E_g - 2E_f/kT}$$

Take ln.

$$1.79 = E_g - 2E_f/kT$$

$$1.79 kT = E_g - 2E_f$$

$$1.78 \times 10^{-3} \times 1.38 \times 10^{-23} \times 300$$

$$1.6 \times 10^{-19}$$

$$= 0.04636 \text{ eV} = E_g - 2E_f$$

$$2E_f = E_g - \text{"}$$

$$E_f = \frac{E_g - \text{"}}{2}$$

$$E_f = 7 \text{ eV}$$

$$E_f = \frac{1}{2} [7 - 0.04636]$$

$$E_f = 3.52$$

Exclusive Falcon

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10 Calculate the intrinsic concentration of charge carriers in germanium at 300K.  $E_g$  for germanium is 0.67eV. Given  $m_e^*/m_0 = 0.12$  and  $m_p^*/m_0 = 0.28$ ?

Sol:  $T = 300K$ .

$$\frac{m_e^*}{m_0} = 0.12$$

$m_0$

$$\frac{m_p^*}{m_0} = 0.28$$

$$E_g = 0.67eV$$

$$m_e^* = 0.12 \times 1.6 \times 10^{-19}$$

$$m = 9.1 \times 10^{-31}$$

$$m_p^* = 0.28 \times 1.6 \times 10^{-19}$$

$$n_i = 2 \left[ \frac{2\pi kT}{h^2} \right]^{3/2} (m_e^* m_p^*)^{3/4} \exp\left[-\frac{E_g}{2k_B T}\right]$$

①  $T = 250$

$$f_{250} = \frac{1}{1 + \exp\left(\frac{0.045 - 0.55eV}{9.16 \times 10^{-5} \times 250}\right)}$$

$$f_{250} \approx 1$$

②  $f_{200} = \frac{1}{1 + \exp\left(\frac{0.45 - 0.5}{9.16 \times 10^{-5} \times 200}\right)}$

$$f_{200} \approx 1$$



④ The following data refers to a dielectric  $\epsilon_r = 4.94$ ,  $n^2 = 2.69$  where  $n$  is index of refraction. Calculate ratio b/w electronic and ionic polarizabilities of this material?

Sol:-  $\alpha_e = \frac{3}{4\pi\epsilon_0} \frac{(\epsilon_r - 1)}{(\epsilon_r + 2)} q^3$

$$\alpha_e = \frac{3}{4\pi\epsilon_0 (0.529 \times 10^{-10})^3} \frac{(4.94 - 1)}{(4.94 + 2)}$$

$$\alpha_e = 1.293 \times 10^{-30} \text{ Cm}^2/\text{V}$$

ionic polarizability

$$\alpha_i = \frac{1}{4\pi\epsilon_0} \frac{(n^2 - 1)}{(n^2 + 2)} q^3$$

$$\alpha_i = \frac{1}{4\pi\epsilon_0 (0.529 \times 10^{-10})^3} \frac{(2.69^2 - 1)}{(2.69^2 + 2)}$$

$$\alpha_i = 1.112 \times 10^{-30} \text{ Cm}^2/\text{V}^2$$

$$\alpha_e = 1.293 \times 10^{-30}$$

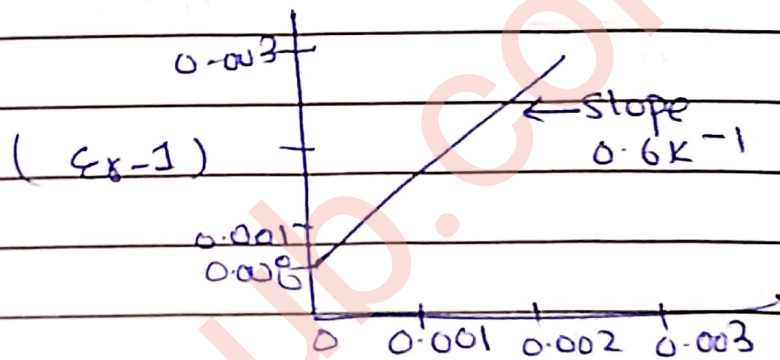
$$\alpha_i = 1.112 \times 10^{-30}$$

$$\frac{\alpha_e}{\alpha_i} = 1.162$$

⑤ The variation of dielectric constant of methyl amine ( $\text{CH}_5\text{N}$ ) as a function of temperature plot as figure (i). Calculate the <sup>permanent</sup> dipole moment and polarizability of molecules. Number of molecules  $\text{m}^{-3}$  may be assumed to be  $2.5 \times 10^{25}$ ?

Sol<sup>n</sup> -

The intercept is 0.008  
and slope is 0.6



$$\text{Now } \epsilon_0 (\epsilon_r - 1) = N (d_e + d_i) \quad \frac{1}{T}$$

$$d_e + d_i = \frac{\epsilon_0 (\epsilon_r - 1)}{N}$$

$$" = \frac{8.85 \times 10^{-12} (0.008)}{2.5 \times 10^{25}}$$

$$\therefore \epsilon_r - 1 = 0.008$$

$$d_e + d_i = 2.84 \times 10^{-40} \text{ Fm}^2$$

$$\frac{N \mu_0^2}{3 k_B \epsilon_0} = \text{slope}$$

$$\mu_0^2 = \frac{3 \times \text{slope} \times \epsilon_0 \times k_B}{N}$$

$$" = \frac{0.6 \times 8.85 \times 10^{-12} \times 3 \times 1.39 \times 10^{-23}}{2.5 \times 10^{25}}$$

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$$\mu_0 = 2.97 \times 10^{-30} \text{ C-m}$$

## Exam Preparation Questions:-

### Assignment # 03:-

Q1) Indicate on an energy level diagram the conduction and valance band, donor and acceptor states. Where are the positions of Fermi level (i) An intrinsic semiconductor. (ii) n-type (iii) P-type semiconductor?

Ans:- n-type P-type

{ electrons are in excess amount in conduction band }

